

## 1.1 – Introduction to Systems of Linear Equations

A **linear equation** can be expressed in the form

$$a_1x_1 + a_2x_2 + \cdots + a_nx_n = b$$

where  $a_i$  are constants, not all zero, and  $b$  is a constant.

14. In each part, use parametric equations to describe the solution set of the linear equation.

a.  $x + 10y = 2$

b.  $x_1 + 3x_2 - 12x_3 = 3$

c.  $4x_1 + 2x_2 + 3x_3 + x_4 = 20$

d.  $v + w + x - 5y + 7z = 0$



b.

$$2x - y + 2z = -4$$

$$6x - 3y + 6z = -12$$

$$-4x + 2y - 4z = 8$$

The following are **elementary row operations** performed on a matrix.

1. Multiply a row by a nonzero constant.
2. Interchange two rows.
3. Add a constant times one row to another.

A **solution** of a linear system is a sequence of  $n$  numbers  $s_1, s_2, \dots, s_n$  that when substituted for corresponding unknowns  $x_i$  makes each equation a true statement. If  $n = 2$ , then the solution is an **ordered pair**, and if  $n = 3$ , it is an **ordered triple**. In general, an **ordered  $n$ -tuple** has the form  $(s_1, s_2, \dots, s_n)$ .

A linear system is **consistent** if it has at least one solution.

A linear system is **inconsistent** if it has no solutions.

20. Find all values of  $k$  for which the given augmented matrix corresponds to a consistent linear system.

a.  $\begin{bmatrix} 3 & -4 & k \\ -6 & 8 & 5 \end{bmatrix}$

b.  $\begin{bmatrix} k & 1 & -2 \\ 4 & -1 & 2 \end{bmatrix}$

Ex: A 3-7-9 diet calls for 3 units of fat, 7 units of protein, and 9 units of carbs in each meal. Suppose an individual has three possible foods to choose from to meet these requirements. Each ounce of the food contains

Food 1: 3 units of fat, 4 units of protein, and 1 unit of carbs

Food 2: 2 units of fat, 5 units of protein, 3 units of carbs

Food 3: 4 units of fat, 1 unit of protein, 2 units of carbs

Let  $x$ ,  $y$ , and  $z$  denote the number of ounces of the first, second, and third foods that a person will consume at the main meal. Find a linear system in  $x$ ,  $y$ , and  $z$  whose solution tells how many ounces of each food must be consumed to meet the diet requirements.